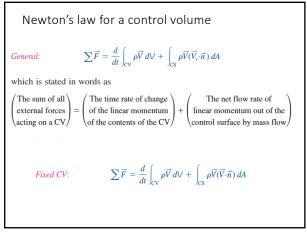


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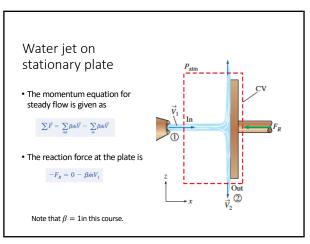
$$\sum \vec{F} = \frac{d}{dt} \int_{\text{sys}} \rho \vec{V} \, dV$$

 Therefore, Newton's second law can be stated as the sum of all external forces acting on a system is equal to the time rate of change of linear momentum of the system.

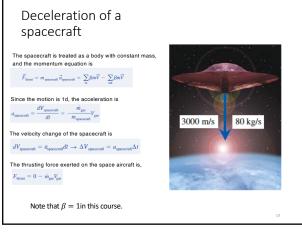
• Applying the Reynolds transport theorem we find:

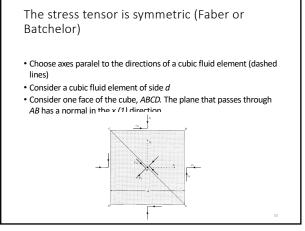
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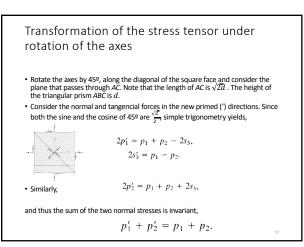
$$\frac{\vec{P}}{dt} \Big|_{\text{sys}} = \frac{d}{dt} \int_{\text{CV}} \rho \vec{V} \, dV + \int_{\text{CS}} \rho \vec{V} \, (\vec{V}_r \cdot \vec{n}) \, dA$$

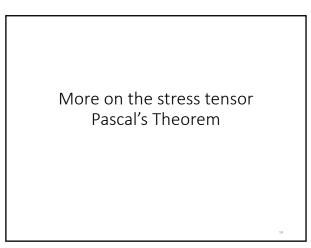


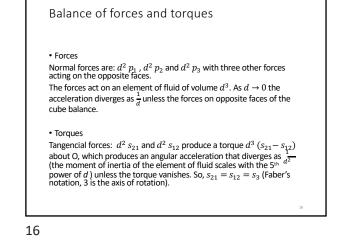


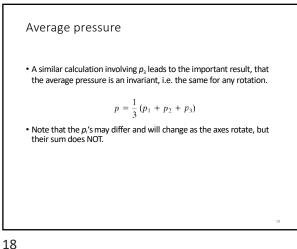


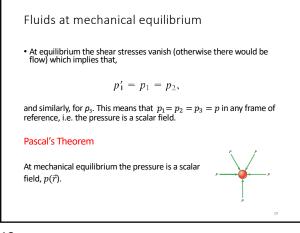


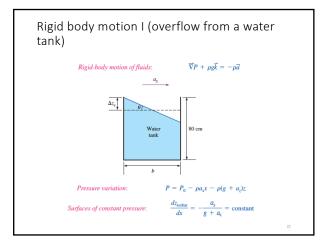


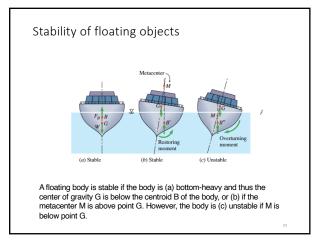


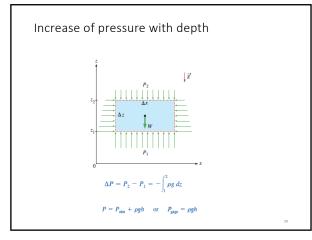


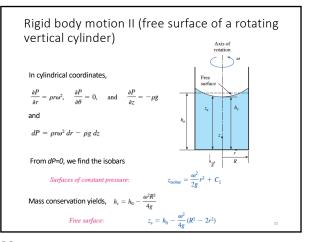




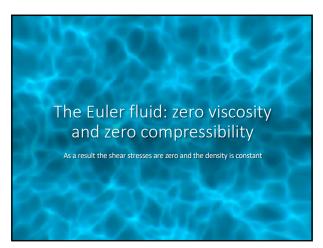


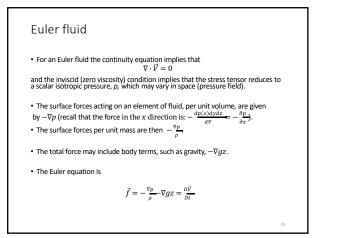




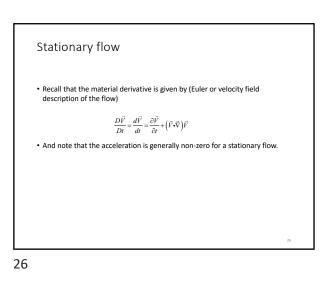


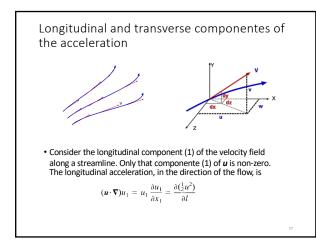


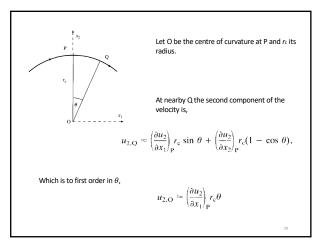


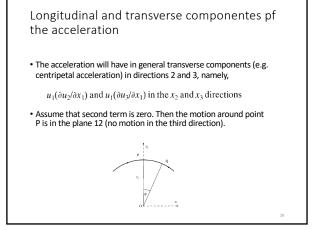




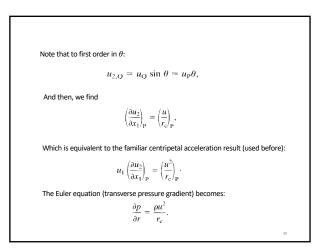


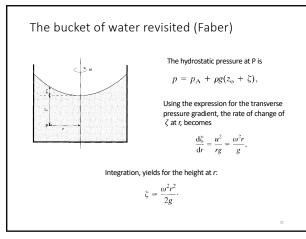


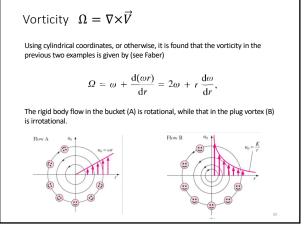






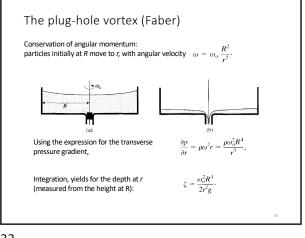




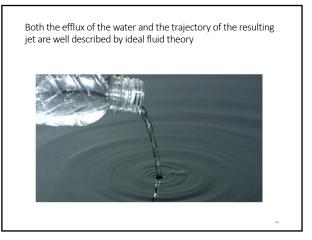








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Bernoulli equation

The longitudinal (along a streamline) component of the acceleration $\partial (\frac{1}{2}u^2)/\partial I$, and that of the force $1 \frac{\partial p}{\partial x} = \partial(gz)$

and that of the force $-\frac{1}{\rho}\frac{\partial \rho}{\partial l}-\frac{\partial (gz)}{\partial l}$.

may be integrated along the streamline, to give

$$\frac{p}{\rho} + gz + \frac{1}{2}u^2 = \text{constant}.$$

which is known as the Bernoulli equation. Note that the constant of integration may (and will in general) depend on the streamline.

